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# Using Bayesian Networks to quantify the reliability of a subsea system in the early design

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# The content

## Background

State of subsea

Reliability modelling and quantification

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## Proposed approach

Introduction to Bayesian Networks

Intended application

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## Illustrative example

Model

Results and discussion

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## Concluding remarks

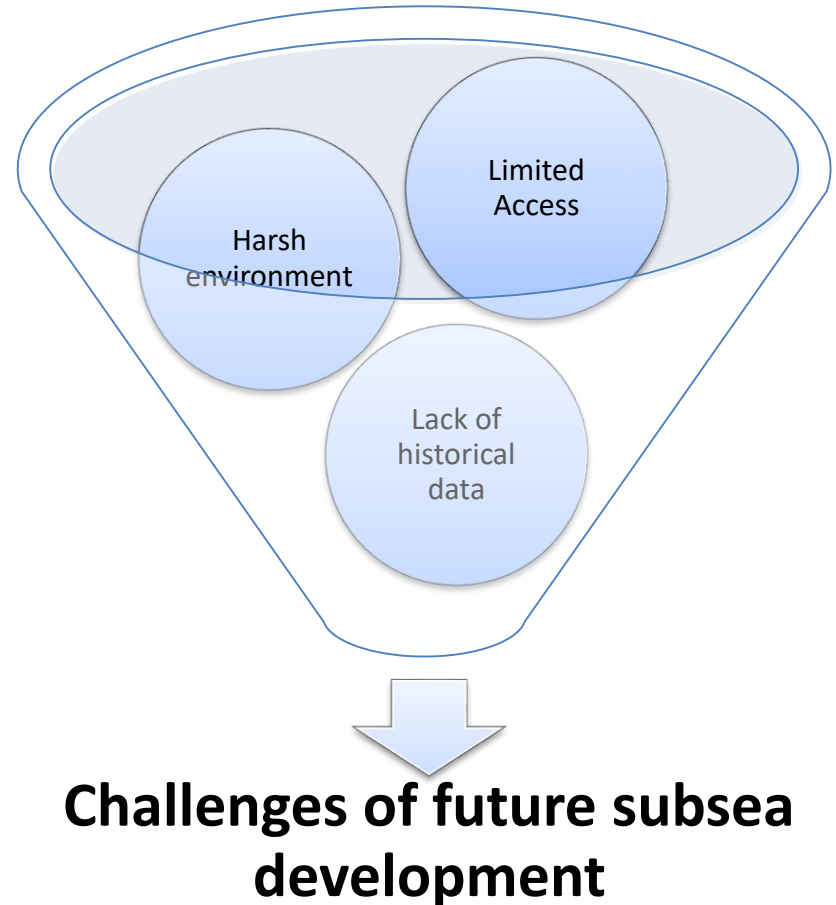
Conclusion

Further work

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Source: Aker Solution (2015)

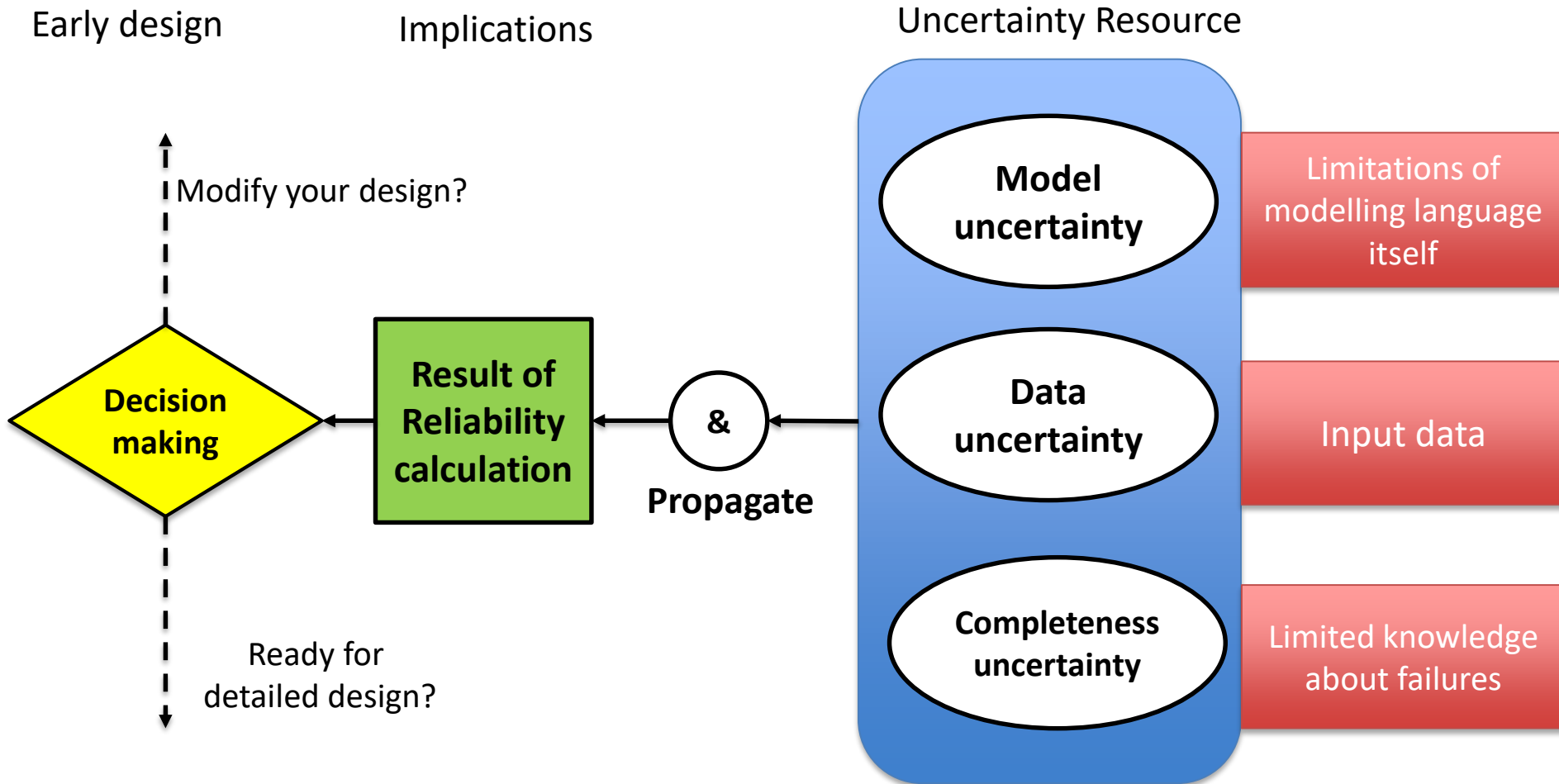


## Challenges of future subsea development

### Motivation:

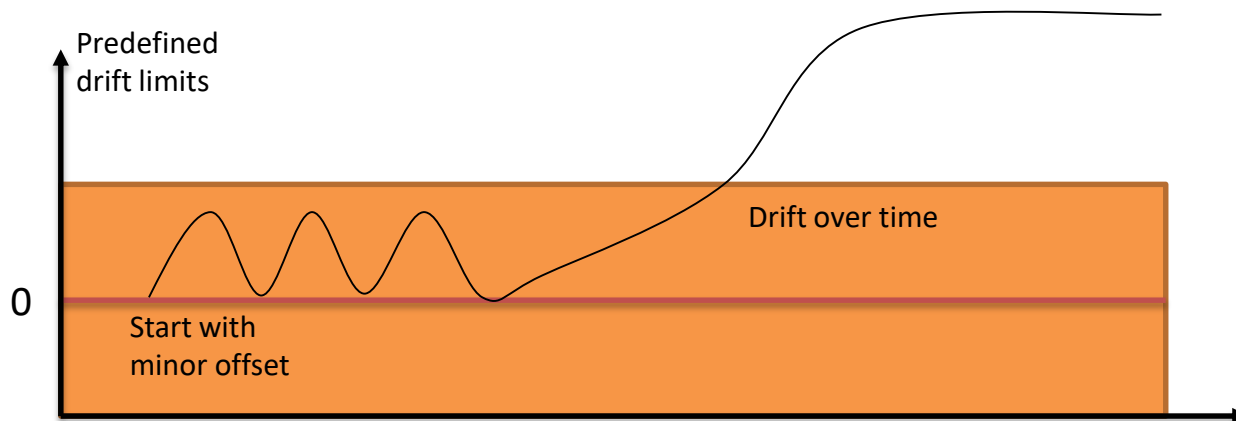
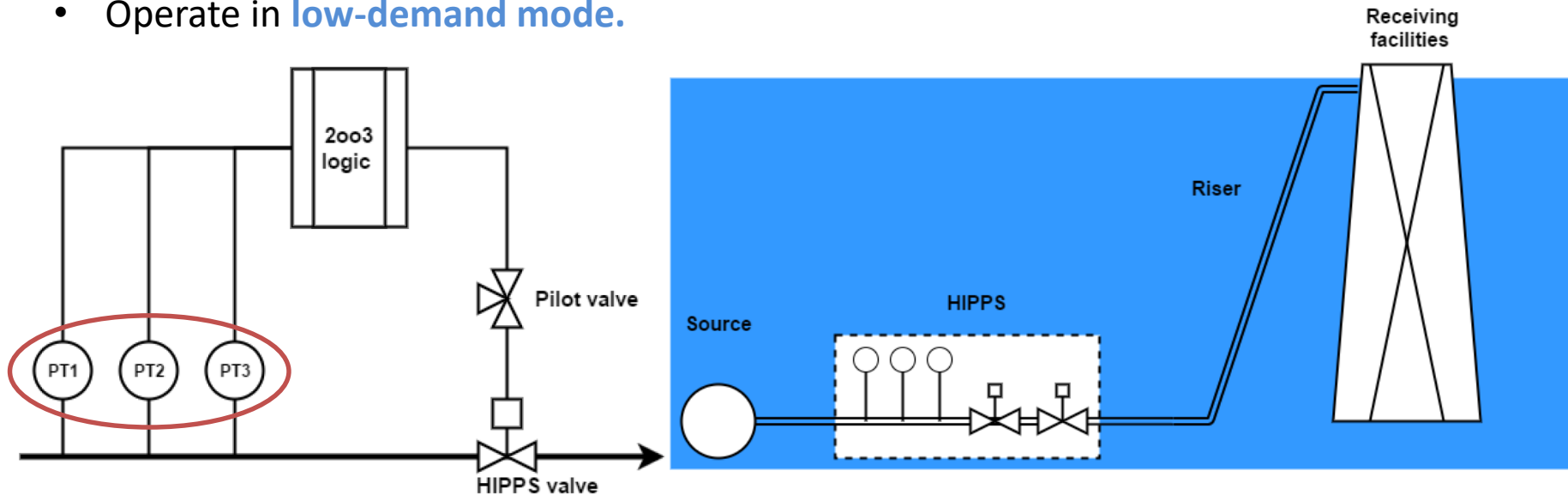
Call for a (new) approach to address foreseeable situations of subsea systems in the **early design**.

In the early design, **high-level uncertainty** is involved in many aspects.

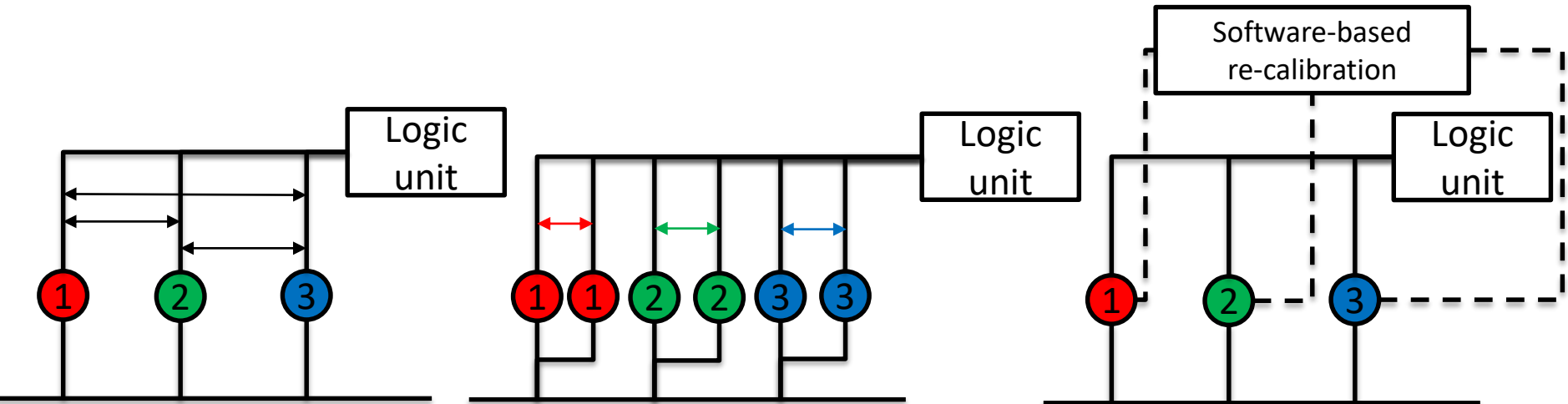
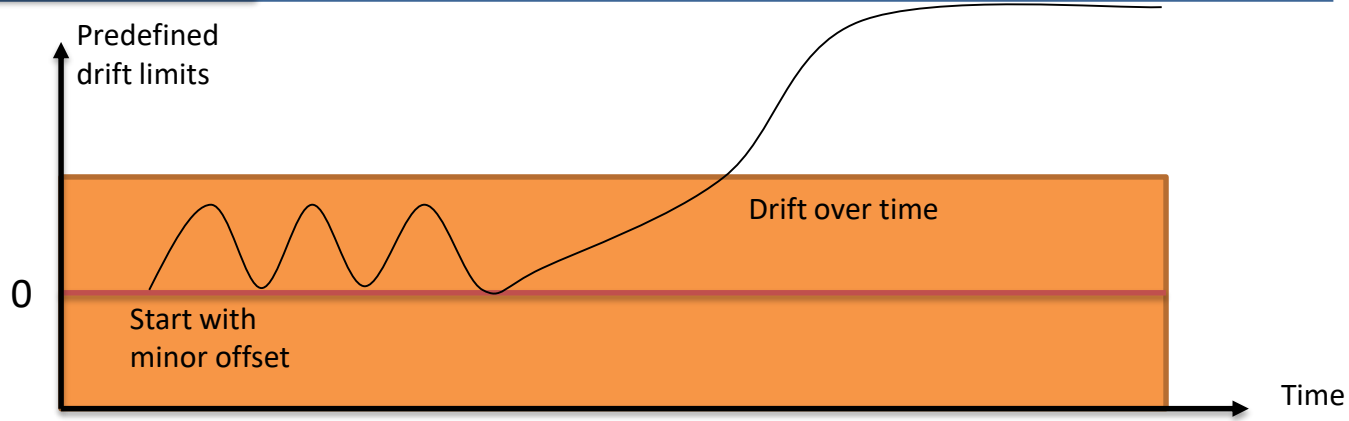


**High integrity pressure protection system (HIPPS):**

- Located at **subsea** to de-rated the design pressure of long pipeline.
- Operate in **low-demand mode**.



1. Leading to the reading offset
2. Influenced by various factors
3. May experience different magnitude at the same time



#### Objective:

Provide an approximation for reliability of sensor in the early design, considering the effect of sensor drift.

## ISO/TR 12489 (2013): reliability modelling and calculation

Approaches	Features
Analytical formula	<ul style="list-style-type: none"> <li>When complexity and redundancy is limited</li> </ul>
Boolean approaches (e.g. Fault Tree Analysis, Reliability Block Diagram)	<ul style="list-style-type: none"> <li>Graphical features</li> </ul>
Markovian approach	
Petri-net (PN) approach	<ul style="list-style-type: none"> <li>A deep understanding of dynamic behaviour of model</li> <li>Better approximation of reality</li> </ul>
Bayesian Networks	<ul style="list-style-type: none"> <li>?</li> </ul>

**Current reliability modelling approaches may not suffice for the purpose.**

Bayesian Networks (BNs) is **not new** for reliability assessment.

Title	Authors	Main contributions
Improving the analysis of dependable systems by mapping fault trees into Bayesian networks. 2001	Bobbio, A., Portinale, L., Minichino, M., & Ciancamerla, E.	Introduce how the fault tree can be translated into Bayesian Networks
The use of Bayesian network modelling for main planning in a manu industry.2010	Jones, B., Jenkinson, I., Yang,	Re-estimate the reliability of operational data.
Dynamic safety analysis of systems by mapping Bayesian network. 2013		Approach for procedures
Performance evaluation of subsea BOP control systems using dynamic Bayesian networks with imperfect repair and preventive maintenance. 2013	Cai, B., Liu, Y., Fan, Q., Zhang, Y., Yu, S., Liu, Z., & Dong, X. (2013).	Includes the effect of imperfect repair and preventive maintenance

**Few attempts to use BN for early design phase.**



## Bayesian Networks (BN):

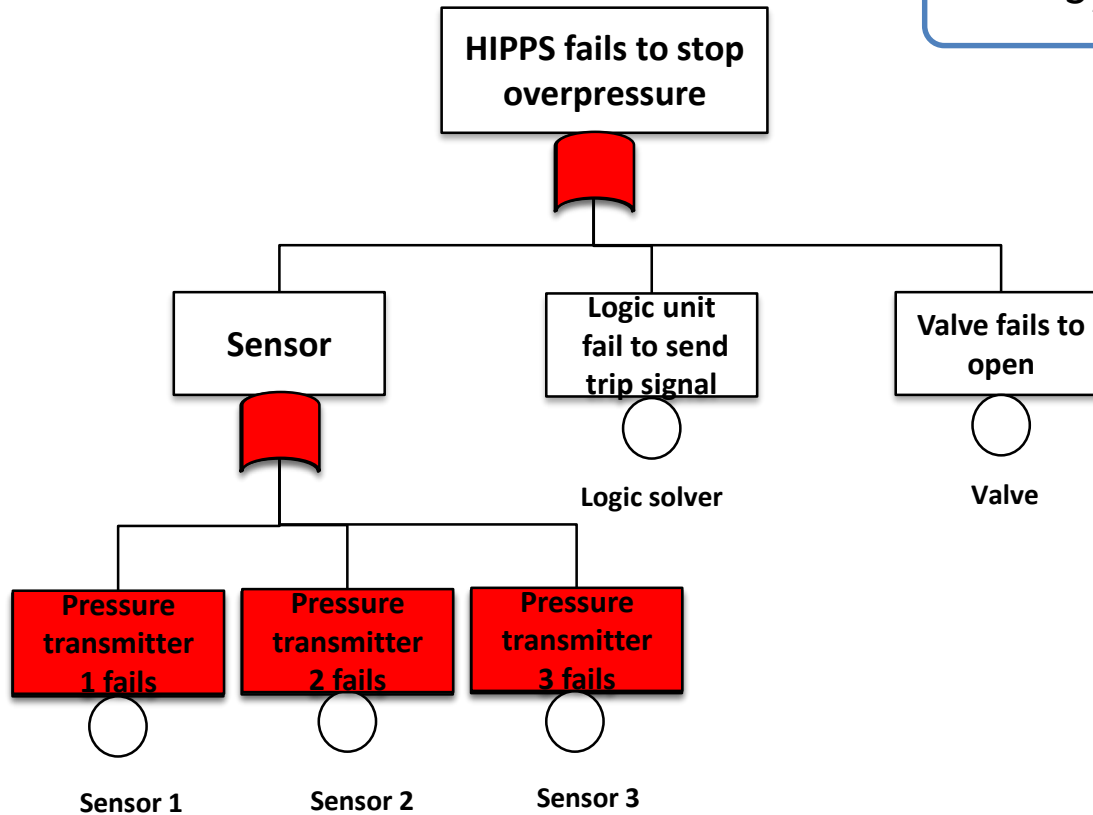
- can be easily **translated from Boolean approaches**, and overcome some restrictions:
  - Involve the probabilistic logic gates and multi-states
  - Model statistical dependencies, e.g. common cause failure
- The ability to **update the estimation** when new information is given:

Bayes' theorem:

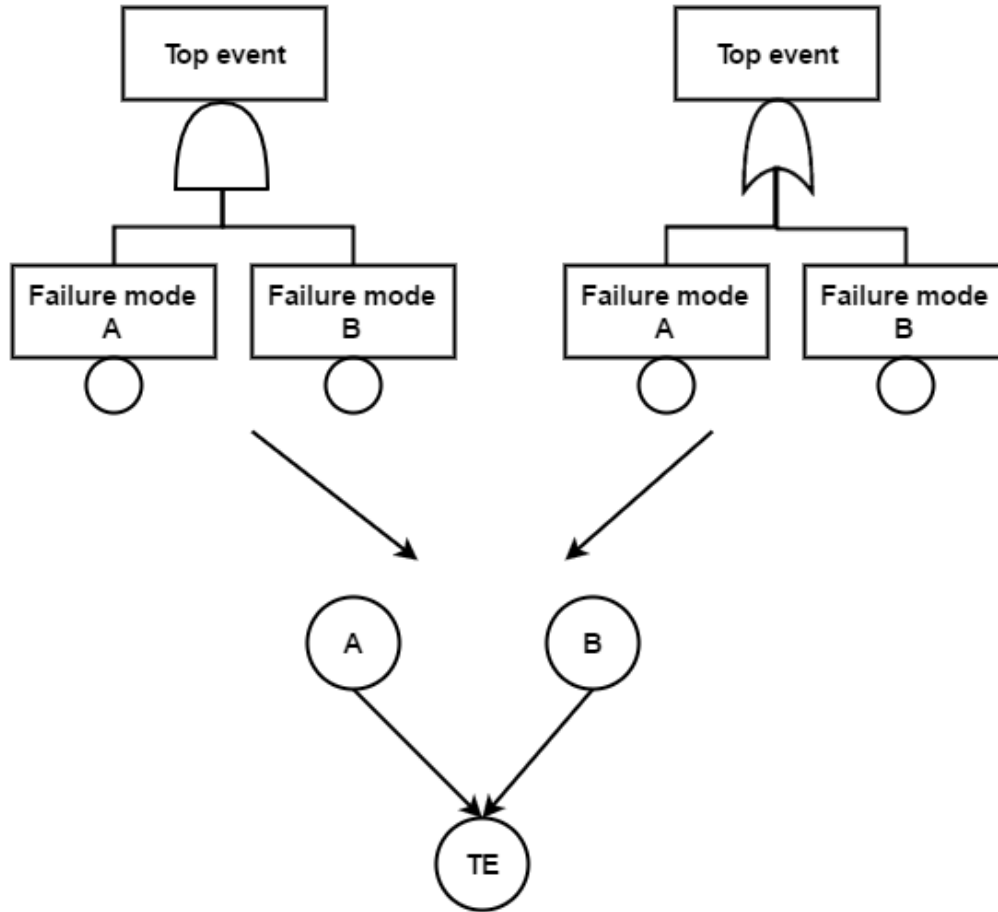
$$Pr(U | E)Pr(E) = Pr(E | U)Pr(U)$$

- The variables can be **probabilistic distributed**, then we can outline the effect of uncertainty, e.g. beta distribution.

System-level



From Fault Tree to Bayesian Networks: probabilistic gate



Same DAG  
But different CPT

For OR-gate:

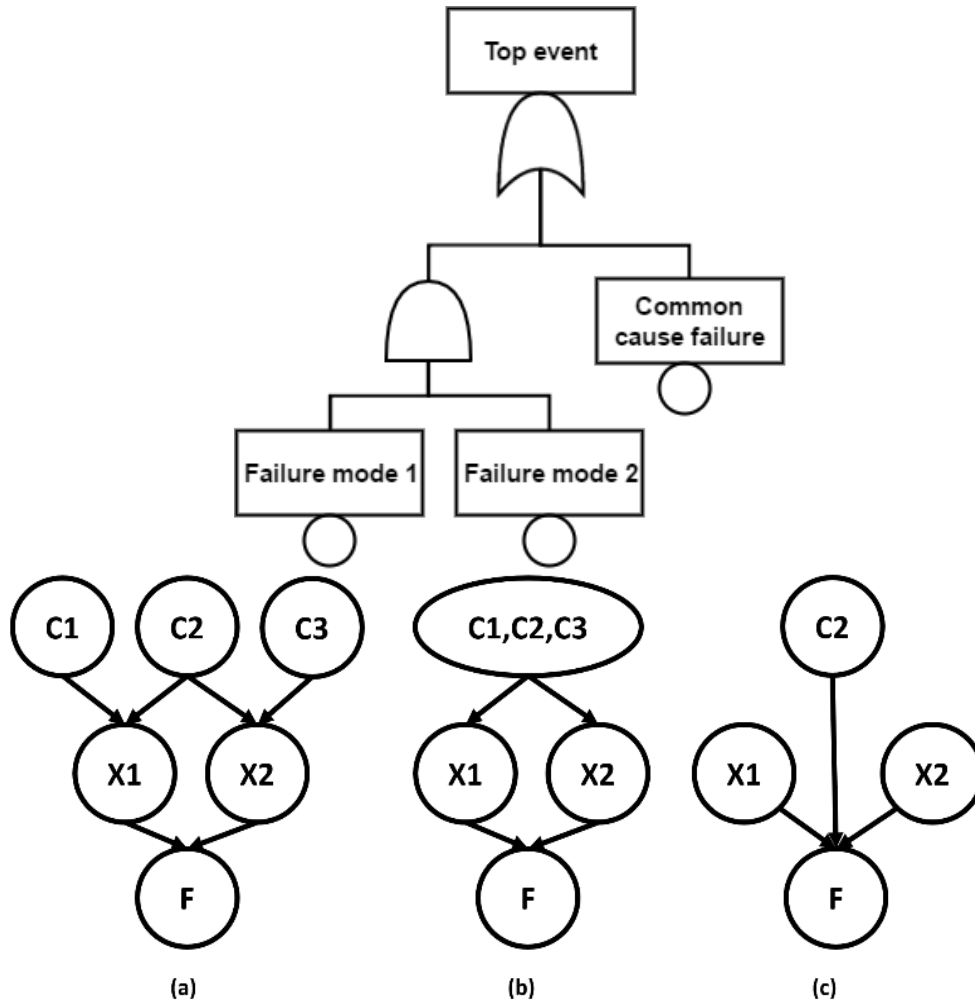
- $\Pr(\text{TE}=1 \mid \text{A}=0, \text{B}=0)=0$
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For AND-gate:

- $\Pr(\text{TE}=1 \mid \text{A}=0, \text{B}=0)=0$
- $\Pr(\text{TE}=1 \mid \text{A}=0, \text{B}=1)=0.001$
- $\Pr(\text{TE}=1 \mid \text{A}=1, \text{B}=0)=0$
- $\Pr(\text{TE}=1 \mid \text{A}=1, \text{B}=1)=1$

Source: Bobbio, A., Portinale, L., Minichino, M., & Ciancamerla, E. (2001)

From Fault Tree to Bayesian Networks: dependencies



In **Fault tree Analysis**, the CCF can be treated implicitly or explicitly, but they may not always give the accurate result.

In **Bayesian Formalism**, the CCF can be modelled by identifying the relationship between failure causes. The inclusion of dependent CCF could be avoided.

(a) Uncorrelated causes, (b) Correlated cause and (c) Common cause  $C_2$

## Bayesian Networks (BN):

- can be easily translated from Boolean approaches, and overcome some restrictions:
  - ❑ Involve the probabilistic logic gates and multi-states
  - ❑ Model statistical dependencies, e.g. common cause failure
- The variables can be **probabilistic distributed**, then we can outline the effect of uncertainty, e.g. beta distribution.
- The ability to **update the estimation** when new information is given:

Bayes' theorem:

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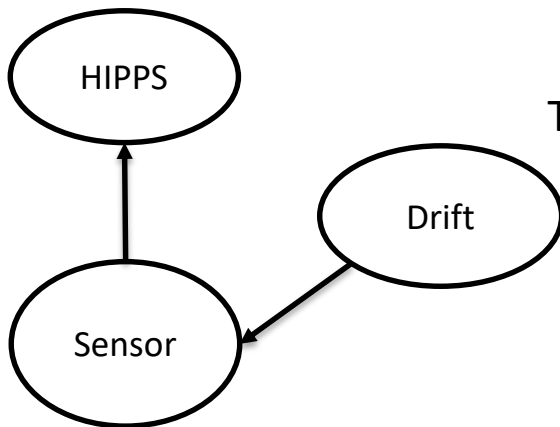
$$Pr(U | E)Pr(E) = Pr(E | U)Pr(U)$$

The simple example for updating, given the observation.

Joint probability for a set of variables:

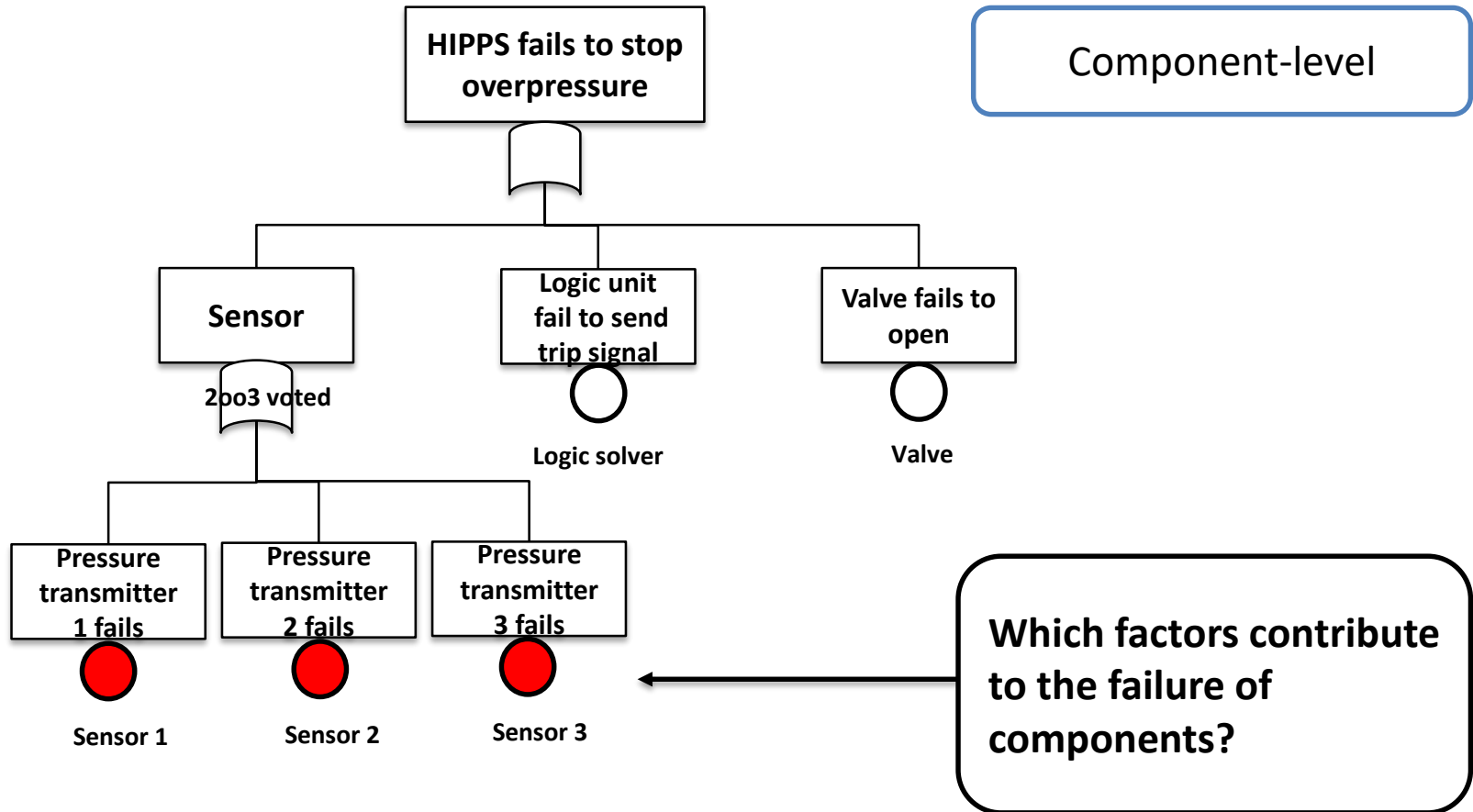
$$Pr(HIPPS, voted, Drift) = Pr(HIPPS | voted) Pr(voted | Drift) Pr(Drift)$$

Observe the failure!



The probability that **Drift** happen, given **HIPPS is failed**:

$$Pr(Drift=T | HIPPS=F) = \frac{\sum_{sensor \in (T,F)} Pr(HIPPS=T, sensor, Drift=T)}{\sum_{Drift, sensor \in (T,F)} Pr(HIPPS=T, sensor, Drift)}$$



Component-level

Which factors contribute to the failure of components?

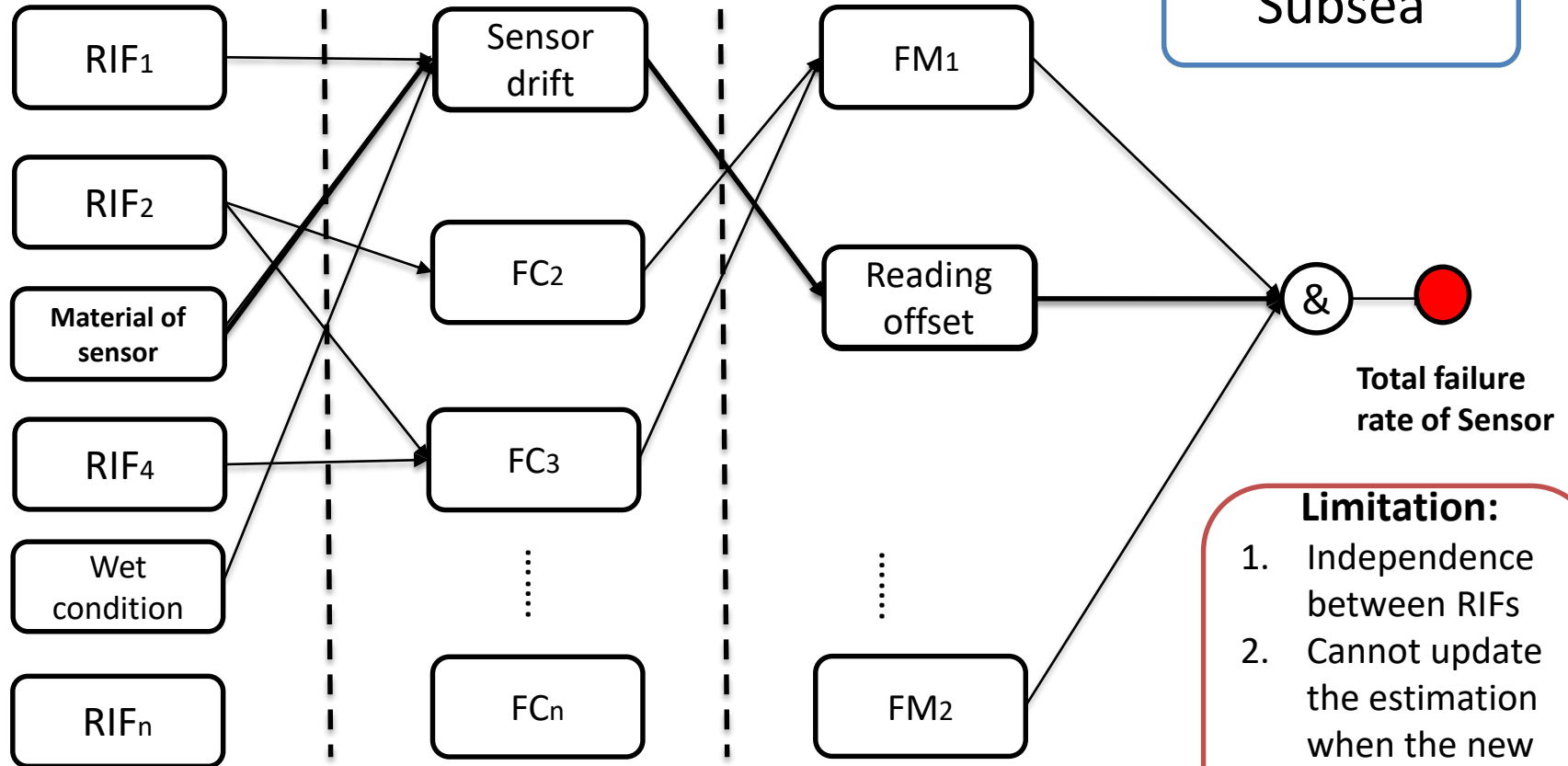
Reliability influence factors (RIFs) are proven to have *theoretical and/or empirical grounded influence* failure. The RIFs will then represent *true likelihood of conditions* that we take into account to the basic events.



Reliability influencing factors (RIFs)

Failure causes (FCs)

Failure mode (FMs)



Source: Maryam Rahimi and Marvin Rausand (2013)

**Limitation:**

1. Independence between RIFs
2. Cannot update the estimation when the new information is given

**Intended use:**

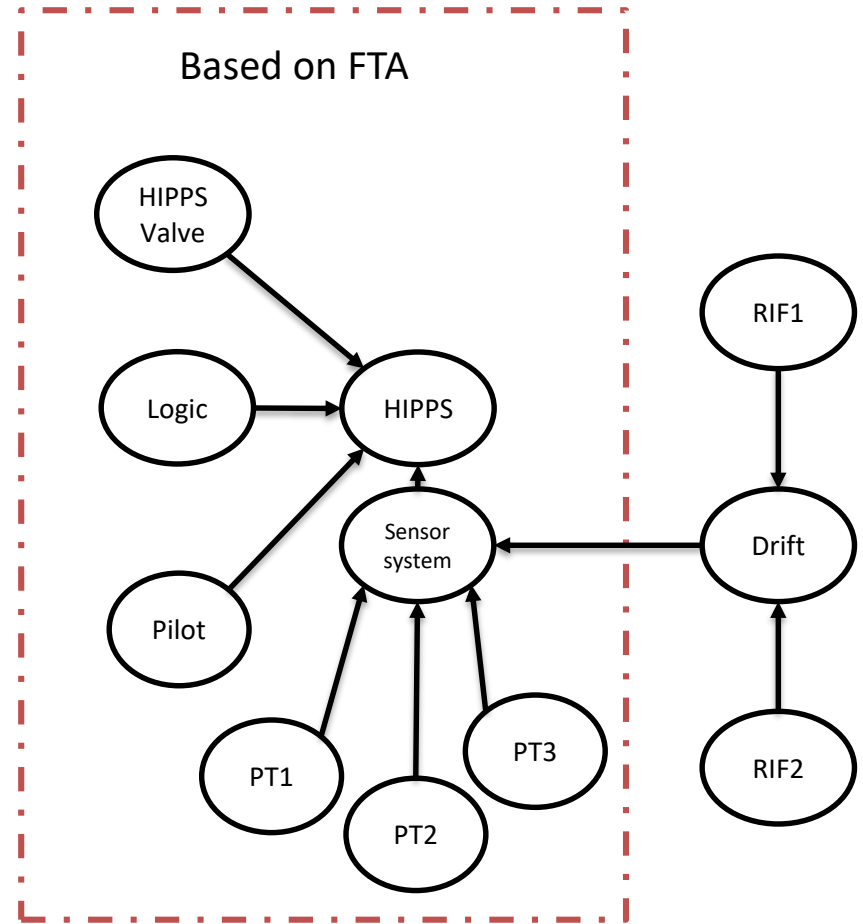
In the early design phase	In the later design phase	In the operational phase
Provide an approximate indication of reliability achievement of subsea innovation	Update the reliability estimates with data from full-scale testing.	Update estimates of the reliability based on forecasting and early detection of changes in trends.

**Proposed use in the early design :**

Allow the flexible inclusion of failure cause that cannot be fully revealed based on historical data.

Assumptions for construct BN model

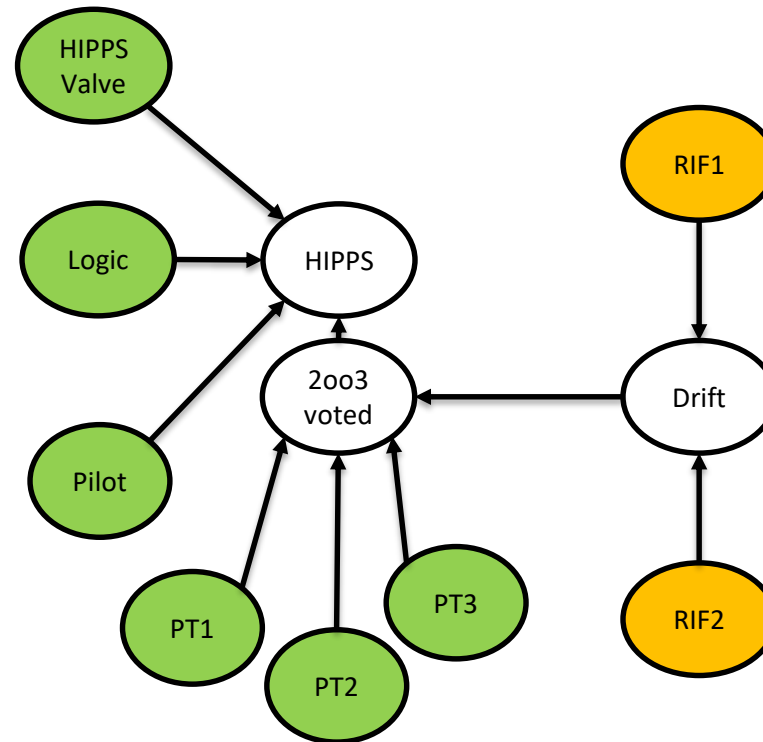
- 1. Sensor drift can impact the voting results.
- 2. The discrete value is assigned for each RIFs.
- 3. The selected RIFs can only influence the magnitude of sensor drift.
- 4. The sensor drift only has the effect on the dangerous failure (not spurious trip)



Simplified BN model for subsea HIPPS

Existing data  
resource:

PDS data  
handbook



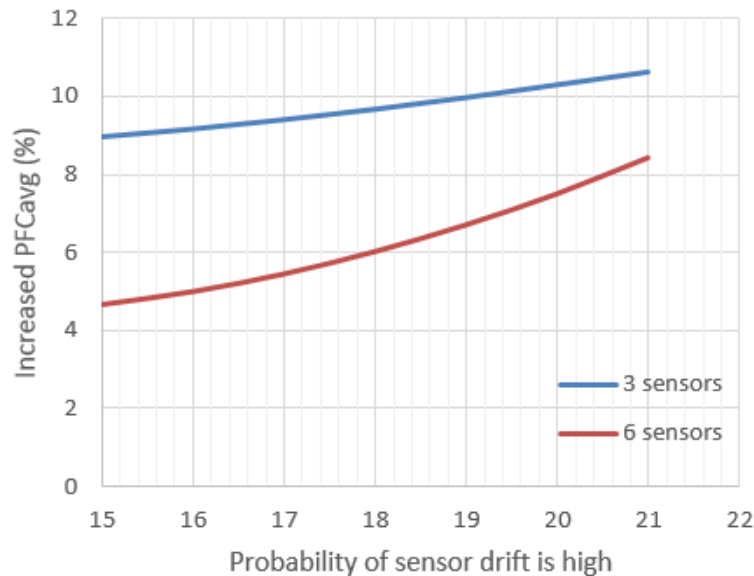
Assign the value of  
RIFs:

- Expert judgement
- Relevance between different applications

The generic RIFs can be found in (Brissaud et al., 2010)

**Main results:**

- When considering the effect of drift, the PFDavg of HIPPS function during the first functional test interval (8760 hours) is now increasing by 8.97%.
- The states of sensor drift can be continuously updated based on the observation of failures. If no calibration, the PFDavg for the next functional test interval will be increased.

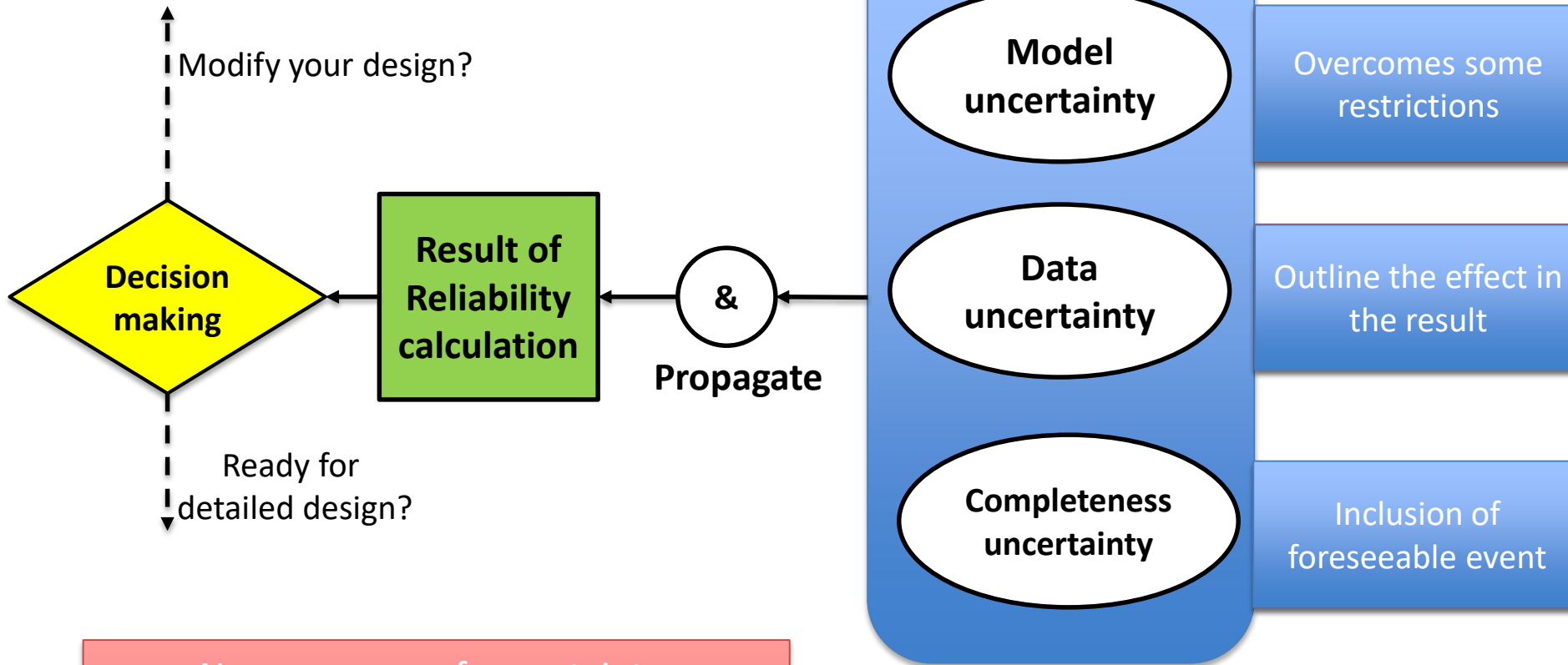


- During the first functional test interval, the most likely configuration is that only the valve is in the faulty state when other parts are functioning, and the probability of MPE is given as 0.004843.

Early design

Implications

Resource



New resource of uncertainty:  
The inherent cause–effect relationship  
between variables

**Conclusion:**

- Provides a preliminary study of how Bayesian Networks can be used to model the specific phenomena (sensors drift):
  - Provides 'approximate' reliability estimates that reflects the best knowledge in the situation.
  - Continuously renewed through evidence collection, e.g. early simulation result.
- The proposed approach could be either simple or advanced, depending on the modelling strategy of different development phase.

**Further work:**

- Propose the new algorithm that adapt the observed data from other applications based on relevance.
- Study the physics behind sensor drift and how it contribute to different types of failures.

# Thank for your attention!



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