

# **Performance Assessment of Redundancy Strategies for Systems Subject to Random Shocks**

**RAMS Seminar**  
**April 7, 2022**

**PhD Candidate: Emefon Dan**

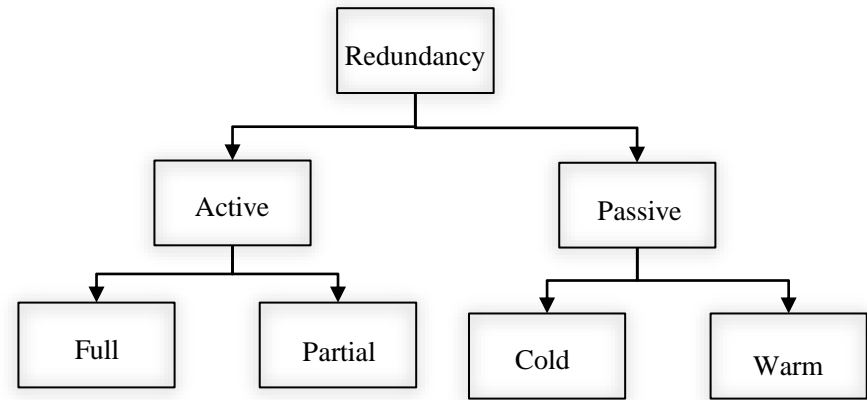
**Supervisors: Prof. Yiliu Liu and Prof. Jørn Vatn**

# Outline

- Introduction
- Objective
- Case study
- Modelling Approach
- Performance assessment results
- Summary
- Further considerations

# Introduction

- Redundancy means the use of two or more items or components to fulfil a specific performance or functional requirement of a system.
- Essential for achieving high system reliability and availability.
- Additional benefit is load sharing between active components.
- Broadly classified into:
  - Active
  - Passive



# Introduction

- Traditional assessment assumes independence.
- Most works that consider dependence mainly focus on failures due to workload.
- In some cases, the system are also subject to random shocks that affect the performance.

## Objective

- Assess the performance of two redundancy strategies for a system that is subject to degradation due to workload and random shocks.

# Case Study – Subsea Multiphase Pumps [1]

- We consider a subsea multiphase pump (MPP) system with 3 pumps installed.
- The system is used to increase the production from subsea oil and gas wells.
- Based on the forecasted production profile, two pumps are sufficient to meet the required capacity from the system.



Fig. Typical subsea field layout with wells connected to a central manifold, a pump station (in red) and a topside facility

Source: Ekerberg et. al.(2022)[1]

# Degradation Mechanism

- Erosion and abrasion due to sand production.
- Sand screens are installed at the wellbore to mitigate wear effects on pumps.
- Continuous sand production erodes the sand screen leading to failure of the sand screen and resulting accidental sand event (shock).
- The sand event has a detrimental impact on the pump performance.

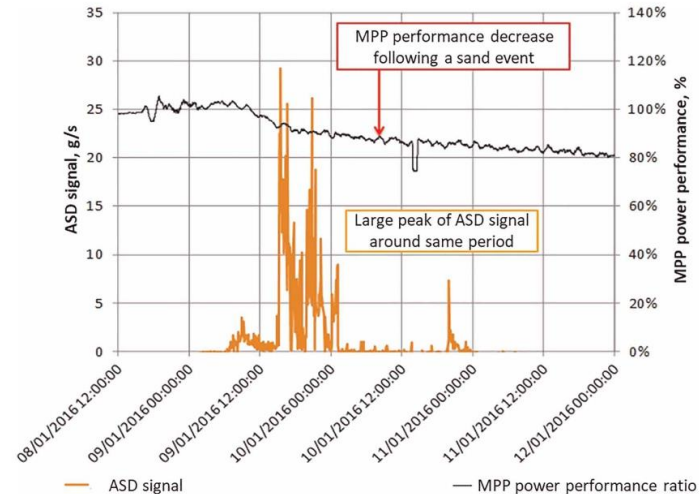


Fig. A transient sand event effect on the MPP performance.  
Source: Ekerberg et. al.(2022)[1]

# Assumptions

- We assume that each pump can contribute 60% towards the required production from the system but depends on the state of the pump.
- Each active pump can be in 3 discrete states:
  - Working (W) – 60%
  - Degraded (D) – 45%
  - Failed (F) – 0%
- Total output from the system depends on number and state of active pumps.
- Random sand events affects all active pumps. The state of the pump is worse after the event.

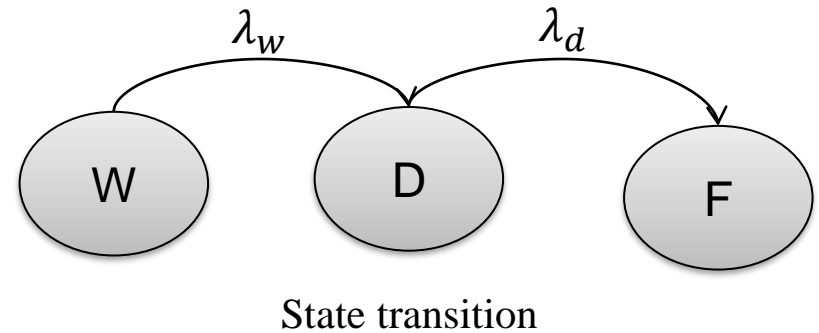
# Assumptions

- In the active redundancy set-up, all 3 pumps are running from the start and share the load.
- In the passive redundancy, 2 pumps share the load from the start while one pump is on standby.
- Standby pump is activated only when required, total output  $< 100\%$ .
- There is a fixed probability, of not being able to activate the standby unit on demand.



# Modelling Framework

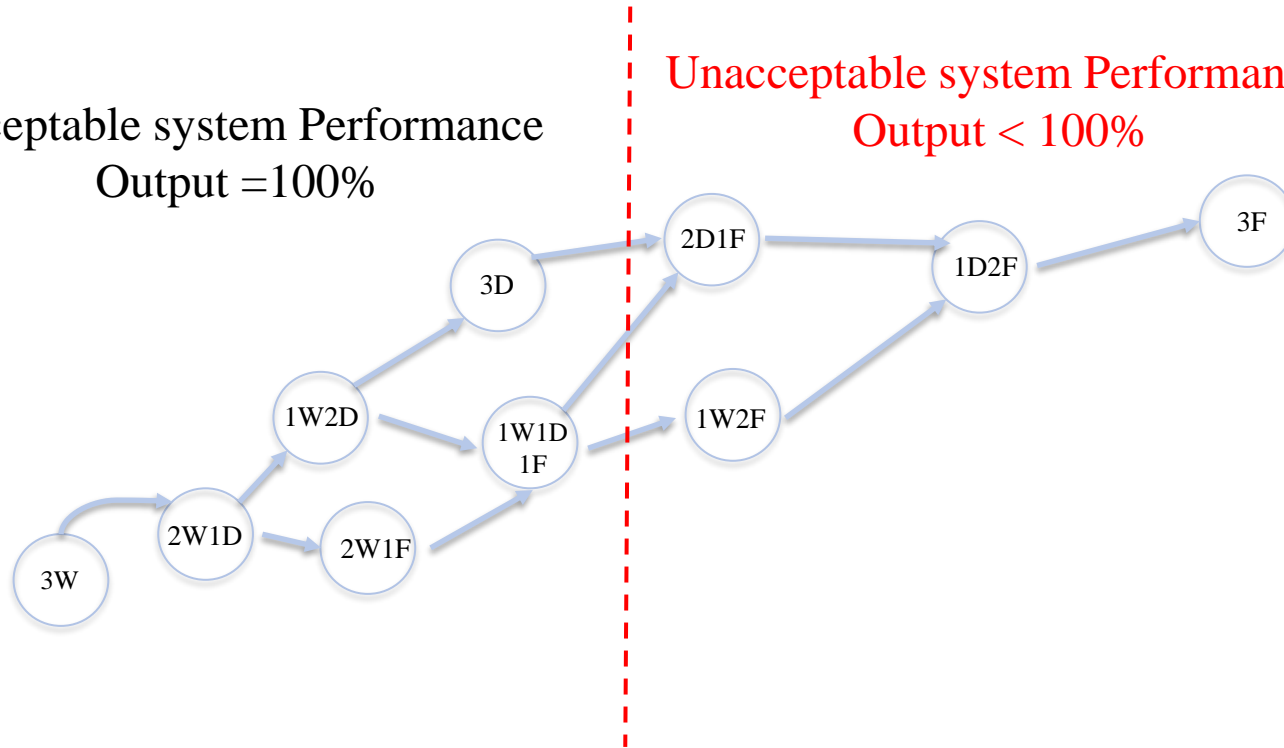
- We assume that transition between discrete states of the pump follows a Markov process with constant transition rates.
  - $\lambda_w$  between W and D
  - $\lambda_d$  between D and F
- The occurrence of random sand events has a constant rate of arrival,  $\lambda_s$ .
- Repair is done on system level and carried out when the total output is below 100.
- There is a deterministic delay before repair.
- Repair is assumed to put the system back in as good as new state.



# Possible transitions (Active)

Acceptable system Performance  
Output = 100%

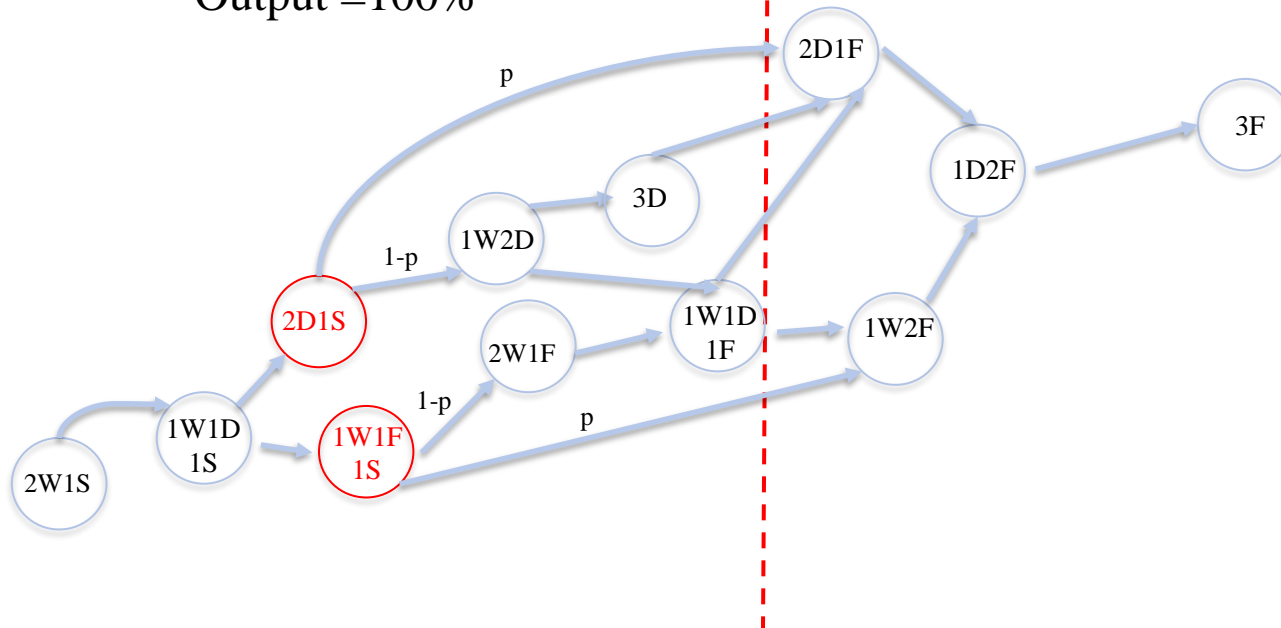
Unacceptable system Performance  
Output < 100%



# Possible transitions (Passive)

Acceptable system Performance  
Output = 100%

Unacceptable system Performance  
Output < 100%



# Dependence modelling

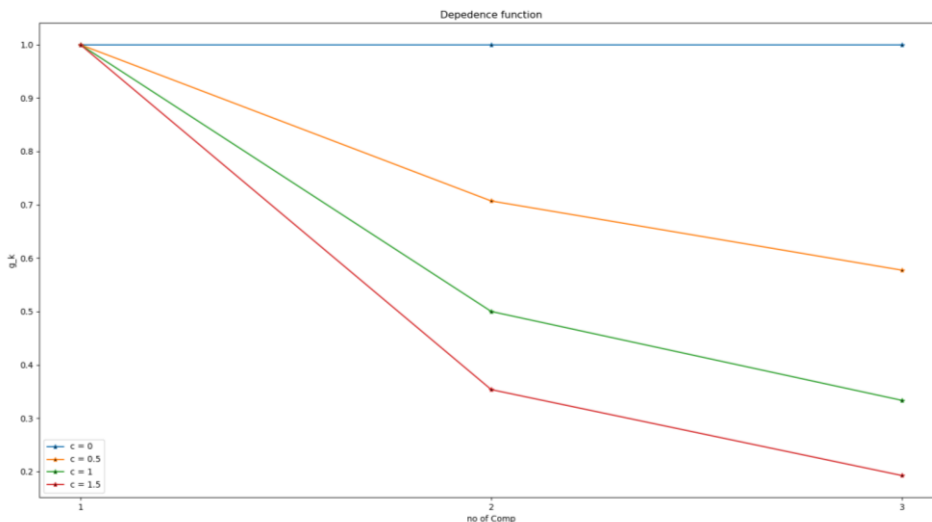
- To incorporate load sharing into our system model, we apply a dependence function.
- Failure rate with  $k$  functioning components is given as:

$$\lambda_0 \cdot g(k)$$

- Where  $g(k)$  is the dependence function defined as:

$$g(k) = \left(\frac{1}{k}\right)^c$$

- $c$  is the load sharing factor. Higher values of  $c$  means that redundant components benefits more from load sharing.
- Some special cases:
  - $c = 0$ . No load sharing
  - $0 < c < 1$ . Weak load sharing
  - $c = 1$ . Proportional load sharing
  - $c > 1$ . Strong load sharing



# Performance Assessment

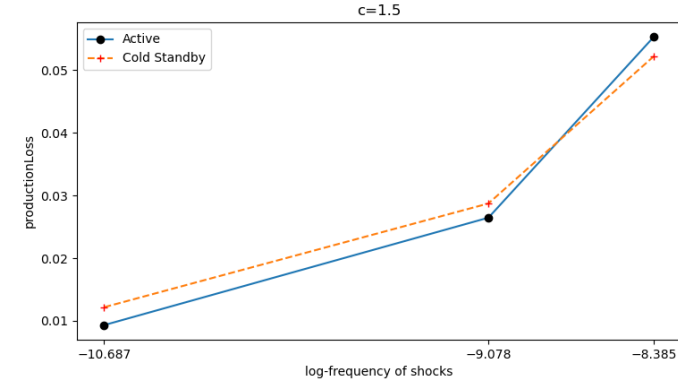
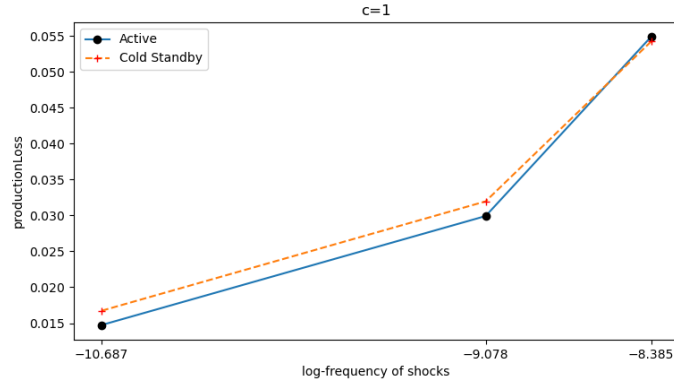
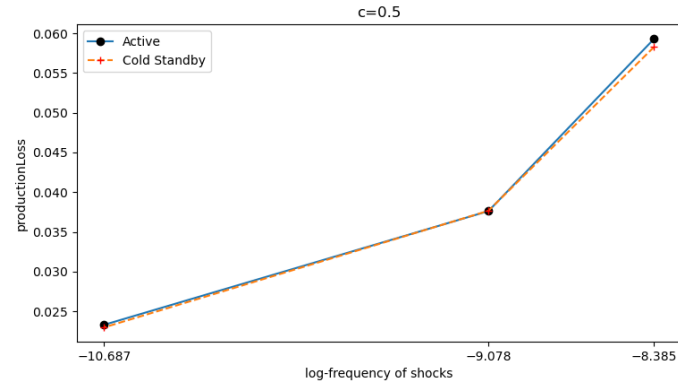
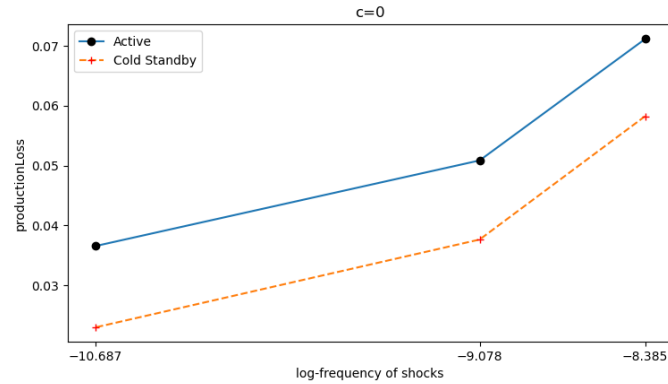
- Average production:

$$\sum_j \theta_j \cdot j$$

- Where  $\theta_j$  is the proportion of time the system spends in states with total output  $j$
- Average Production loss: 100 – Average production
- Frequency of shocks:
  - Once in 5 years (less frequent)
  - Once per year (medium)
  - Twice per year (high frequency)
- Monte-carlo simulation with 20000 simulations.
- Mission time: 5 years

PARAMETER	DESCRIPTION	VALUE
$\lambda_W$	Transition rate from new to degraded state	$2 \times 10^{-4}$
$\lambda_D$	Transition rate from degraded to failed state	$4 \times 10^{-4}$
$p$	Probability of switch failure	0.01
$RD$	Delay before repair	730

# Performance Assessment



# Summary

- Two redundancy strategy is assessed:
  - Active with load sharing
  - Passive with cold standby
- System performance depends on the frequency of shocks to the system but also on the degree of load sharing.
- For low frequency of shocks, active redundancy strategy has a better performance than passive redundancy especially when the degree of load sharing is high ( $c \geq 1$ )
- For high frequency of shocks, the passive redundancy has a better performance

# Further works

- Consider a continuous degradation model. How to incorporate load sharing into such model.
- Find the optimal maintenance strategy with this model.



# References

1. Ekeberg, I., Bibet, P., Knudsen, H., Reimers, Ø., and Torbergsen, E. (2022). Sand management and erosion prediction in subsea multiphase pumps. *Journal of the Global Power and Propulsion Society*, 6, pp.24-38.  
<https://doi.org/10.33737/jgpps/145322>
2. Yu, H., Chu, C., Châtelet, È. and Yalaoui, F., 2007. Reliability optimization of a redundant system with failure dependencies. *Reliability Engineering & System Safety*, 92(12), pp.1627-1634.
3. Olde Keizer, M. C. A., et al. (2018). "Condition-based maintenance for systems with economic dependence and load sharing." *International Journal of Production Economics* **195**: 319-327.

**Thank you**