

A New Availability Allocation Method

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Background

- Motivation and objective
- Proposed approach
- Availability - assumptions

Proposed method

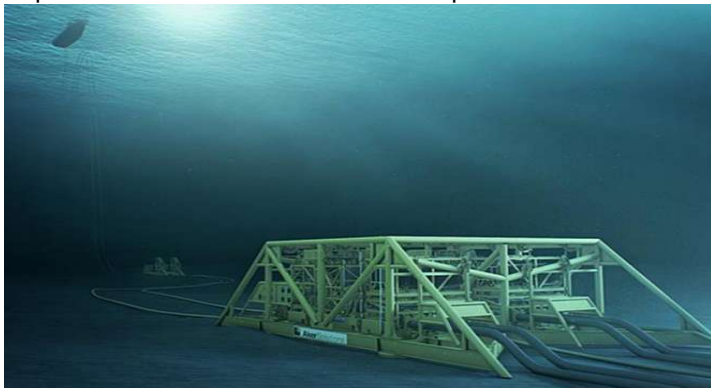
- Varying cost function
- Varying cost function (procedure)
- Identical cost function and complexity as a cost function

Conclusion

Further work

- ▶ Availability (A) is the ability of the system to be in a state where the specified functions are (or can be) carried out.
- ▶ The availability targets are often set in an early design phase, and will be the reference point for the selection of design solution and operational strategy.
- ▶ In situations where the target is not met, it is important to improve the reliability and restoration time of individual components such that the target is met.
- ▶ However, any availability improvement involves increasing in cost, complexity and size.

In the early design phase, it may be important that availability improvement is done with minimum possible effort.



Source:

Åsgard subsea compression system

- ▶ A suitable allocation method is thus applied such that the availability target is allocated to the individual components within a given constraint (such as cost).
- ▶ However, most availability allocation methods are complex and resource demanding such as heuristic, meta-heuristic and dynamic programming and so on.
- ▶ Such complex methods are not so practical because
 - ▶ availability allocation is performed in the early design phase where only little knowledge about the system is available,
 - ▶ results from the allocation process are not definite, but are guidelines to support the decision needs to be made by taking into account several other engineering aspects, such as previous experience, flexibility in case of changing operating and environmental conditions, and regulations; and
 - ▶ regular reliability engineers may not be familiar with such mainstream optimization methods.
- ▶ The main objective of this paper is therefore to develop a simple and user-friendly method.

- ▶ Simple and user-friendly methods for reliability allocation for non-repairable system have long been used, such as
 - ▶ Equal apportionment
 - ▶ ARINC
 - ▶ AGREE
 - ▶ Minimum Effort Algorithm
- ▶ The proposed approach here is to adopt the **Minimum Effort Algorithm** for availability allocation.
- ▶ The advantage of using Minimum Effort Algorithm is that it optimizes the allocation with minimum effort.
- ▶ Three allocation options are proposed depending on the objective of the allocation and availability of cost data:
 1. Allocation with identical cost/complexity function over components
 2. Allocation with varying cost function
 3. Allocation based on complexity of components for improvement

- ▶ Only unplanned downtime due to critical item failure is considered
- ▶ Exponentially distributed time to failure with parameter λ and time to restoration with parameter μ are assumed. And MTTF and MTTR are the respective means. Thus, for item i

$$A_i = \frac{\text{MTTF}_i}{\text{MTTF}_i + \text{MTTR}_i} = \frac{\mu_i}{\lambda_i + \mu_i} \quad (1)$$

- ▶ The system is assumed to be expressed by n critical components connected in series. Thus, the system availability is

$$A = \prod_{i=1}^{i=n} \frac{\mu_i}{\lambda_i + \mu_i} \approx \left(1 + \sum_{i=1}^n \sigma_i \right)^{-1} \quad (2)$$

where $\sigma_i = \lambda_i M_i$ is the current unavailability contribution of component i . For brevity purpose we use M instead of MTTR.

Let C_{λ_i} and C_{M_i} be respectively the cost to increase the mean time to failure and to increase the restoration rate of component i per hour, for $i = 1, 2, \dots, n$. The cost functions will then be

$$h_i(\lambda_i, \lambda_i^a) = C_{\lambda_i} (\text{MTTF}_i^a - \text{MTTF}_i) \quad (3)$$

$$g_i(M_i, M_i^a) = C_{M_i} (\mu_i^a - \mu_i) \quad (4)$$

The allocation is to minimize the total improvement cost (TC) subject to the constraint of achieving the availability target, i.e.

$$\begin{aligned} \text{Min } TC &= \sum_{i=1}^n h_i(\lambda_i, \lambda_i^a) + \sum_{i=1}^n g_i(M_i, M_i^a) \\ \text{Subject to } &A_i^a = A^t \end{aligned} \quad (5)$$

where a and t stand for allocated and target respectively.

1. Arrange the current unavailability contributions in descending order, i.e. $\sigma_1 \geq \sigma_2 \geq \sigma_3 \cdots \geq \sigma_n$.

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2. Determine k weakest components that need to be improved, and that can be done by finding the maximum value of i such that

$$\sigma_i > \frac{U_t - \sum_{i=i+1}^{n+1} \sigma_i}{i} = \psi_i \quad (6)$$

where $\sigma_{n+1} = 0$ and $U_t = 1/A^t - 1$.

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3. The allocated unavailability contributions are

$$\sigma_i^a = \begin{cases} \psi_i & i \leq k \\ \sigma_i & i > k \end{cases} \quad (7)$$

Assumptions:

- ▶ The effort needed to improve low-reliability components is less than that of the effort needed to improve high-reliability components.
- ▶ It is economically infeasible to allocate a reliability for a component higher than the reliability of any other component.

4. Calculate the unavailability contribution reduction factor for component i , i.e. $\beta_i = \sigma_i^a / \sigma_i$.

- Calculate the unavailability contribution reduction factor for component i , i.e. $\beta_i = \sigma_i^a / \sigma_i$.
- Calculate the relative reliability and restoration time improvement costs as

$$r_{\lambda_i} = \frac{C_{\lambda_i}^2}{(C_{\lambda_i} + C_{M_i}) \sum_{i=1}^k C_{\lambda_i}}, \quad r_{M_i} = \frac{C_{M_i}^2}{(C_{\lambda_i} + C_{M_i}) \sum_{i=1}^k C_{M_i}} \quad (8)$$

In situations where

- ▶ there is no room (or desire) for improvement for the failure rate or the restoration time of a component, the value of the associated relative cost (r) should be one.
- ▶ improvement is known to be impossible (or undesired) for *both* the failure rate and restoration time of a component, the following modification is necessary. Suppose no improvement is allowed for component l , the unavailability contribution reduction factors should be adjusted as

$$\beta_i^* = \frac{k \cdot \sigma_k^a - \sigma_l}{\sigma_i}, \quad i \neq l \quad (9)$$

6. Determine θ_i such that

$$\beta_i = (r_{\lambda_i} \cdot r_{M_i})^{\theta_i} \Rightarrow \theta_i = \frac{\ln(\beta_i)}{\ln(r_{\lambda_i} r_{M_i})} \quad (10)$$

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7. The allocated λ and M will then be

$$\lambda_i^a = r_{\lambda_i}^{\theta_i} \lambda_i, \quad M_i^a = r_{M_i}^{\theta_i} M_i \quad (11)$$

and the rest $n - k$ remain unchanged.

- ▶ These two are special cases of the varying-cost function.
- ▶ In situations where no improvement cost data is available or the cost is not relevant to be considered, allocation with *identical cost function* can be used.
 - ▶ From immediately step four above, the allocated reliability and restoration time can be calculated as

$$\lambda_i^a = \beta_i^{0.5} \lambda_i, \quad M_i^a = \beta_i^{0.5} M_i \quad (12)$$

- ▶ If accurate cost data is unavailable or estimating absolute total improvement cost is of less relevance, it may be important to estimate costs relative to each other (i.e. Z), rather than in absolute values. And r becomes

$$r_{\lambda_i} = \frac{Z_{\lambda_i}^2}{(Z_{\lambda_i} + Z_{M_i}) \sum_{i=1}^k Z_{\lambda_i}}, \quad r_{M_i} = \frac{Z_{M_i}^2}{(Z_{\lambda_i} + Z_{M_i}) \sum_{i=1}^k Z_{M_i}} \quad (13)$$

- ▶ The paper proposed an allocation method that minimizes the total improvement cost.
- ▶ The effort can be
 - ▶ equal for all components
 - ▶ varying and expressed in absolute values, or
 - ▶ varying but expressed based on the level complexity/difficulty to make an improvement
- ▶ Qualitative aspects of components are crucial to decide on the prioritization of components for improvement. The method is capable of accommodating such aspects through the complexity score (Z) that can be assigned by expert judgment.

- ▶ The method is suitable in the early design phases of product development to identify the most economically and technically feasible alternative to carry out availability improvement.
- ▶ The most important advantage of the proposed approach is that the minimum effort algorithm has been used by regular engineers for reliability allocation, so that it would not take much effort for engineers to understand and implement the proposed extension.
- ▶ Numerical compared with an existing method is made and the result indicated that the proposed method provides a reasonably accurate result given its simplicity to use.

The following are identified as areas for further research work:

- ▶ The paper utilized complexity scores (Z) without discussing in detail what factors to be considered and how.
- ▶ The focus has only been on production systems. It is thus important to adopt the method for safety systems.
- ▶ Availability allocation for complex systems with complex operational philosophies require advanced algorithms. It would be beneficial to evaluate the efficiency of the proposed method by comparing it with advanced algorithms using a more realistic and complex system.